

## CLAIM AMENDMENTS

Claim 1 (currently amended): A method of identifying a user, comprising the steps of:

a) selecting, by the user, a modulus  $p$  from the group of equations consisting of:

$$p=(2^{dk}-2^{rk}-1)/r,$$

where  $0<2c\leq d$ , where  $r \neq$  does not equal 1, and where  $GCD(c,d)=1$ ;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where  $d$  is even, and where  $k$  is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{rk}-1)/r,$$

where  $3d<6c<4d$ , and where  $GCD(c,d)=1$ ;

$$p=(2^{dk}-2^{rk}+1)/r,$$

where  $0<2c\leq d$ , where  $r \neq$  does not equal 1, and where  $GCD(c,d)=1$ ; and

$$p=(2^{4k}-2^{3k}+2^{2k}+1)/r;$$

- b) selecting, by the user, an elliptic curve  $E$  and an order  $q$ ;
- c) selecting, by the user, a basepoint  $G$ ;
- d) generating, by the user, a private key  $w$ ;
- e) generating, by the user, a public key  $W=wG$ ;
- f) distributing, by the user,  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;
- g) ~~retrieving~~ generating, by a prover, the prover's private key  ~~$w$~~   $w_p$  and public key  ~~$W$~~   $W_p$   
and distributing  $W_p$ ;
- h) retrieving, by a verifier, the prover's public key  ~~$W$~~   $W_p$ ;
- i) generating, by the prover, a private integer  ~~$k$~~   $k_p$ ;
- j) combining, by the prover,  ~~$k$~~   $k_p$  and ~~the prover's~~  $G$  to form  $K$  using the form of the  
prover's modulus  $p$ ;
- k) sending, by the prover,  $K$  to the verifier;
- l) sending, by the verifier, a challenge integer  $c$  to prover;
- m) combining, by the prover,  $c$ ,  ~~$k$~~   $k_p$ , and  ~~$w$~~   $w_p$  to form a response integer  $v$ ;
- n) sending, by the prover,  $v$  to the verifier; and
- o) combining, by the verifier,  $cG$ ,  $K$ , and  ~~$W$~~   $W_p$  using the form of the ~~prover's~~ modulus  $p$   
and checking to see if the combination is equal to  $vG$ , if so the user is identified as the user,  
otherwise the user is not identified as the user.

Claim 2 (currently amended): The method of ~~generating a digital signature claim 1. further~~  
comprising the steps of:

a) ~~selecting a modulus  $p$  from the group of equations consisting of:~~

$$p = (2^{dk} - 2^{rk} - 1) / r,$$

~~where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ;~~

$$p = (2^{dk} - 2^{(d-1)k} + 2^{(d-2)k} - \dots - 2^k + 1) / r,$$

~~where  $d$  is even, and where  $k$  is not equal to  $2 \pmod{4}$ ;~~

$$p = (2^{dk} - 2^{rk} - 1) / r,$$

~~where  $3d < 6c \leq 4d$ , and where  $GCD(c, d) = 1$ ;~~

$$p = (2^{dk} - 2^{rk} + 1) / r,$$

~~where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ; and~~

$$p = (2^{dk} - 2^{rk} + 2^{rk} + 1) / r,$$

- ~~— b) selecting an elliptic curve  $E$  and an order  $q$ ;~~
- ~~— c) selecting a basepoint  $G$ ;~~
- ~~— d) generating a private key  $w$ ;~~
- ~~— e) generating a public key  $W = wG$ ;~~
- ~~— f) distributing  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;~~

ga) ~~retrieving~~ generating, by a signer, the signer's private key  ~~$w$~~   $w_s$ ;

hb) generating, by the signer, a private integer  ~~$k$~~   $k_s$ ;

ic) combining, by the signer,  ~~$k$~~   $k_s$  and  $G$  to form  $K$  using the form of the ~~prover's~~ modulus

$p$ ;

jd) combining, by the signer,  $K$  and a message  $M$  to form an integer  $h$ ;

ke) combining by the signer,  $h$ ,  ~~$k$~~   $k_s$ , and  ~~$w$~~   $w_s$  to form an integer  $s$ ; and

lf) sending, by the signer,  $M$  and  $(K, s)$  as a digital signature of  $M$ .

Claim 3 (currently amended): The method of claim 1, further including the steps of:

- a) retrieving, by the verifier, the prover's public key  ~~$W$~~   $W_p$ ;
- b) receiving, by the verifier,  $M$  and  $(K, s)$ ;
- c) combining, by the verifier,  $K$  and  $M$  to form an integer  $h$ ; and

d) combining, by the verifier,  $h$ ,  $k$ ,  $K$ , and  $W$   $W_p$  using the form of the prover's modulus  $p$  and checking to see if the combination is equal to  $sG$ , if so then the digital signature is verified, otherwise the digital signature is not verified.

Claim 4 (currently amended): The method of ~~generating a digital signature~~ claim 1, further comprising the steps of:

a) ~~selecting a modulus  $p$  from the group of equations consisting of:~~

$$p = (2^{dk} - 2^{rk} - 1) / r,$$

~~where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ;~~

$$p = (2^{dk} - 2^{(d+k)k} + 2^{(d+2k)k} - \dots - 2^k + 1) / r,$$

~~where  $d$  is even, and where  $k$  is not equal to  $2 \pmod{4}$ ;~~

$$p = (2^{dk} - 2^{rk} - 1) / r,$$

~~where  $3d < 6c < 4d$ , and where  $GCD(c, d) = 1$ ;~~

$$p = (2^{dk} - 2^{rk} + 1) / r,$$

where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ; and

$$p = (2^{4k} - 2^{2k} + 2^{2k} + 1) / r;$$

- ~~\_\_\_\_\_ b) selecting an elliptic curve  $E$  and an order  $q$ ;~~
- ~~\_\_\_\_\_ c) selecting a basepoint  $G$ ;~~
- ~~\_\_\_\_\_ d) generating a private key  $w$ ;~~
- ~~\_\_\_\_\_ e) generating a public key  $W = wG$ ;~~
- ~~\_\_\_\_\_ f) distributing  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;~~

ga) retrieving generating, by a signer, the signer's private key  ~~$w$~~   $w_s$ ;

hb) generating, by the signer, a private integer  ~~$k$~~   $k_s$ ;

ic) combining, by the signer,  ~~$k$~~   $k_s$  and  $G$  to form  $K$  using the form of the ~~prover's~~ modulus

$p$ ;

jd) combining, by the signer,  $K$  and a message  $M$  to form an integer  $h$ ;

ke) combining by the signer,  $h$ ,  ~~$k$~~   $k_s$ , and  ~~$w$~~   $w_s$  to form an integer  $s$ ; and

lf) sending, by the signer,  $M$  and  $(h, s)$  as a digital signature of  $M$ .

Claim 5 (currently amended): The method of claim 4, further including the steps of:

a) retrieving, by the verifier, the prover's public key  ~~$W$~~   $W_p$ ;

- b) receiving, by the verifier,  $M$  and  $(h,s)$ ;
- c) combining, by the verifier,  $h$ ,  $\cancel{W} \underline{W}_p$ , and  $sG$  using the form of the ~~prover's~~ modulus  $p$  to form  $K$ ;
- d) combining, by the verifier,  $K$  and  $M$  to form an integer  $h'$ ; and
- e) checking, by the verifier, that  $h$  is equal to  $h'$ , if so then the digital signature is verified, otherwise the digital signature is not verified.